

Roll Number: _____

Thapar University, Patiala
Department of Computer Science and Engineering

EST

Course Code: UCS406

B. E. COE, CML,CAG,SEM (Second Year): Semester-IV

Course Name : Data Structures and Algorithms

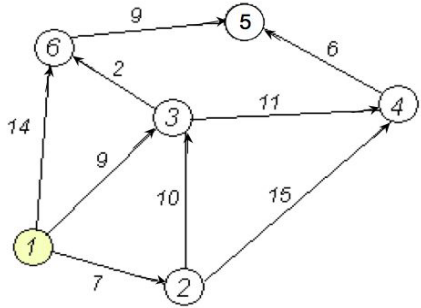
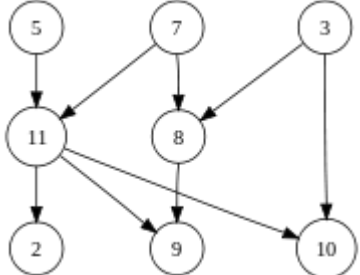
May 19, 2016

Thursday, 9.00 – 12.00 Hrs

Time: 3 Hours, M. Marks: 100

Name of Faculty: DG, RIR, TBH, ANK

Note: All questions are compulsory and attempt all parts of a question at one place.
Assume missing data, if any, suitably. Clearly specify your notations used in algorithms.

Q 1. a)	<p>Write algorithm for matrix-chain product problem using dynamic programming. Apply the same to find an optimal parenthesization of given 5 matrices whose sequence of dimensions is $\langle 4,10,3,12,20,7 \rangle$ i.e $A_1(4 \times 10)$, $A_2(10 \times 3)$, $A_3(3 \times 12)$, $A_4(12 \times 20)$ and $A_5(20 \times 7)$.</p>	(14)															
b)	<p>Apply Dijkstra’s algorithm on the following directed weighted graph. Find out the minimum cost from given source 1 to all the possible destinations.</p> <div style="text-align: center;">  </div>	(6)															
Q 2. a)	<p>Write algorithm for 0-1 knapsack problem using dynamic programming. Apply the same to find optimal items in the Knapsack in the following example and show all the intermediate steps. Consider 4 items along their respective weights and values</p> <table border="1" style="margin: auto; border-collapse: collapse; text-align: center;"> <thead> <tr> <th>Item i</th> <th>Value v_i</th> <th>Weight w_i</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>15</td> <td>1</td> </tr> <tr> <td>2</td> <td>10</td> <td>5</td> </tr> <tr> <td>3</td> <td>9</td> <td>3</td> </tr> <tr> <td>4</td> <td>5</td> <td>4</td> </tr> </tbody> </table> <p>The maximum capacity of the knapsack is $W = 8$. Fill the knapsack such that knapsack should not exceed its maximum capacity and it should have maximum profit value.</p>	Item i	Value v_i	Weight w_i	1	15	1	2	10	5	3	9	3	4	5	4	(14)
Item i	Value v_i	Weight w_i															
1	15	1															
2	10	5															
3	9	3															
4	5	4															
b)	<p>Arrange the nodes of the following Directed Acyclic Graph using Topological Sort.</p> <div style="text-align: center;">  </div>	(6)															

<p>Q 3. a)</p> <p>b)</p>	<p>Write algorithm for n queen problem using backtracking approach. Discuss your algorithm step wise for a 4x4 chess board.</p> <p>Find the complexity of the following:</p> <ol style="list-style-type: none"> 1. $T(n) = 4T(n/2) + \log n$ 2. $T(n) = 3T(n/3) + n/2$ 3. $T(n) = 3T(n/4) + n \log n$ 	<p>(14)</p> <p>(6)</p>
<p>Q 4. a)</p> <p>b)</p>	<p>Define the TSP problem. Find the minimum cost tour in the following graph using Branch and Bound approach.</p> <div style="text-align: center;"> <pre> graph TD 1((1)) -- 3 --> 2((2)) 2 -- 4 --> 1 1 -- 2 --> 3((3)) 3 -- 1 --> 1 2 -- 4 --> 3 3 -- 8 --> 2 </pre> </div> <p>Considering inserting the keys 20 32 41 14 25 38 27 98 69 into a hash table of length $m = 11$ using open addressing with the primary hash function $h(k) = k \bmod m$. Illustrate the result of inserting these keys using linear probing, using quadratic probing and using double hashing with $h'(k) = 1 + (k \bmod (m-1))$.</p>	<p>(10)</p> <p>(10)</p>
<p>Q 5. a)</p> <p>b)</p> <p>c)</p> <p>d)</p> <p>e)</p>	<p>Compare P, NP and NP-complete.</p> <p>Differentiate among Divide and conquer, Dynamic Programming and backtracking.</p> <p>Define Queue and its possible operations.</p> <p>Differentiate between BFS and DFS.</p> <p>Discuss memory representations of a graph with suitable example.</p>	<p>(20)</p>